

## A SEISMIC ANALYSIS OF SEGMENTAL TUNNEL LINING USING ARTIFICIAL ACCELERATION

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### Abstract

This paper aims to generate a set of artificial accelerations by using PG02 program, based on Yamamoto's regression equations and response spectrum of Vietnamese National Standard TCVN 9386-2012 condition. Taking the obtained ground motion as input data to calculate the tunnel structure of the project Metro line No.3 (Nhon - Hanoi Railway Station) by program Plaxis2D. The connections among the tunnel segments are replaced by semi-rigid joint under Jassen's assumption. The results show that the peak ground acceleration value can be considered as one of the important factors affecting on the internal force of tunnel besides a number of other acceleration factors (peak ground velocity, root mean square acceleration, intensity of Arias, time duration of strong motion).

*Keywords:* Seismic analysis; segmental lining; artificial acceleration; semi-rigid.

### 1. Introduction

The metro line is an important component of the future urban transport system. The underground sections of these lines are often constructed using TBM. Although underground structures have many advantages compared to above structures when subjected to seismic waves, in fact, there have been many failures of tunnel in the world when they are affected by earthquakes.

The full dynamic analysis of tunnel structures under seismic loads has also been studied by many authors. The recently common trend is to use numerical analysis techniques. Brinkgreve R.B.J. and Broere W. [3], Kontoe et al. [6], Hassash [10], St. John [8], Anh DoNgoc [2]... have used numerical simulations to calculate some types of tunnel structures subjected to seismic loads. The above studies have shown the behavior of the tunnel when subjected to earthquakes but did not pay attention and give an appropriate acceleration spectrum.

This study focuses on using the artificial accelerations, which compatible with Vietnamese National Standard TCVN 9386-2012, to calculate the tunnel structure at Hanoi, a case in Ba Dinh district. These input accelerations are randomly generated by

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PG02, a program based on the Yamamoto’s regression equations [8] and response spectrum matching condition.

## 2. Numerical analysis for segmental tunnel

### 2.1. Objects of research and assumptions

The object selected for the survey is the underground section of the project "Urban Railway (Metro) No.3, Nhon - Hanoi Railway Station" (from station S9 to S12, Figure 1), located at Ba Dinh district. Because the tunnel length is much larger than the other dimensions, it is assumed that the structure modeling is plane deformation problem.



Figure 1. Plan of Metro line No.3 in Hanoi City.

### 2.2. Soil properties

Geology from the ground level to bottom has a thickness of 60m, including 6 geological layers (denoted from L1 to L6). The specific parameters of each layer are given in Table 1. Ground surrounding medium the tunnel is simulated as 15-nodes triangle elements and the Hardening Soil (HS) model is selected. The depth of groundwater is 5m from the ground surface.

Table 1. Table of parameters of soil layers

Row	Parameters	Denote	Layers					
			1	2	3	4	5	6
1	Layer thickness (m)		2.5	15	3.5	15.0	11.0	13.0
2	Model materials		HS	HS	HS	HS	HS	HS
3	Saturated density (kN/m <sup>3</sup> )	$\gamma_{sat}$	18	17.8	19.4	20.0	21.0	23.0
4	Natural density (kN/m <sup>3</sup> )	$\gamma_{unsat}$	17	16.8	19.4	20.0	21.0	23.0
5	Oed-stiffness modulus (kN/m <sup>2</sup> )	$E_{oed}^{ref}$	5,100	3,600	16,200	25,200	48,800	131,000
6	Secant stiffness modulus (kN/m <sup>2</sup> )	$E_{50}^{ref}$	5,100	3,600	16,200	25,200	48,800	131,000

Row	Parameters	Denote	Layers					
			1	2	3	4	5	6
7	Load- unloading Modulus (kN/m <sup>2</sup> )	$E_{ur}^{ref}$	1.53E+04	1.08E+04	4.85E+04	7.55E+04	1.46E+05	3.94E+05
8	Poisson's coefficient	$\nu$	0.3	0.35	0.30	0.30	0.30	0.28
9	Cohesion force (kN/m <sup>2</sup> )	$c$	55	30	0.1	0.1	0.1	0.1
10	Internal friction angle (°)	$\phi$	20	12	31	37	39	45
11	Interactive coefficient	$R_{inter}$	0.8	0.8	0.7	0.7	0.7	0.7

### 2.3. Properties of segmental tunnel lining

The tunnel is placed at a depth of 25 meters from the ground level. Model of segmental tunnel structure material is assumed to be homogeneous and satisfy the linear elastic model, cross-section features of tunnel structure are shown in Table 2.

Table 2. Table of parameters for the tunnel structure

Row	Parameters	Denoted	Values	Units
1	Tunnel diameter (inner/outer)	$D_{in}/D_{out}$	5.7/6.3	m
2	Modulus of elasticity of tunnel concrete	$E_b$	2.5E+7	kN/m <sup>2</sup>
3	Poisson's coefficient for concrete	$\nu$	0.15	
4	Thickness of lining	$t$	0.30	m
5	Height of the connection	$l_t$	0.185	m
6	Width of the tunnel ring	$b$	1.0	m

The paper uses Janssen’s assumptions [5] to model connection among segments of tunnel lining (Figure 2). There,  $C_r$  is elastic jointing anti-bending hardness;  $k_r$  is the elastic link hardness in the radius direction;  $k_t$  is the elastic link hardness in the tangentially direction.

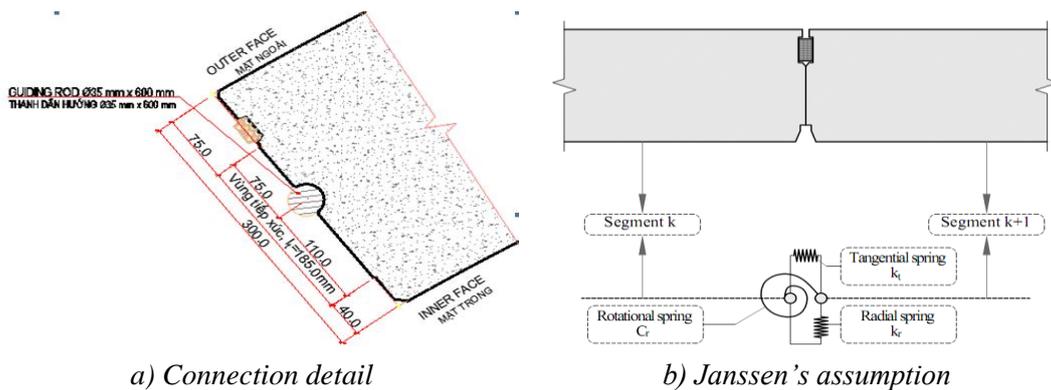


Figure 2. Connection detail and Janssen’s assumption

The values for  $k_r$  and  $k_t$  are often chosen with high values, when using Plaxis 2D, these links are usually ignored in calculation. The main parameter of the Janssen joint [5],

$C_r$ , is determined by formula (1):

$$C_r = \frac{b \cdot l_t^2 \cdot E_c}{12} = \frac{1 \cdot 0,185^2 \cdot 2,5 \cdot 10^7}{12} = 71,302 \text{ (kNm/rad)} \quad (1)$$

where  $l_t$  is the height of the connection (m);  $E_c$  is the elastic module of concrete (kN/m<sup>2</sup>);  $b$  is the width of the tunnel ring (m).

The semi-rigid joints are modelled in Plaxis as a ‘Hinges and rotation springs’, in there, the spring stiffness is  $C_r$  value (Figure 3, Min.Moment =  $-M_{yield} = -150$  kNm; Max.Moment =  $M_{yield} = 150$  kNm [5]).

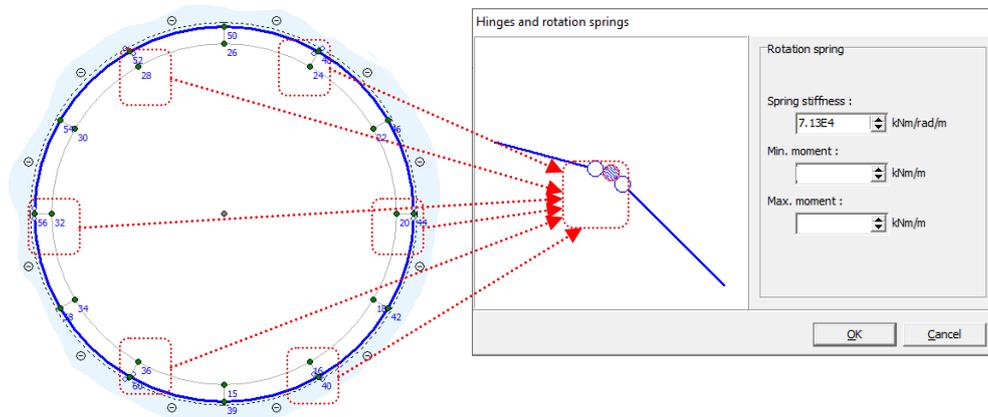


Figure 3. Semi-rigid joint is modeled in the Plaxis 2D software

Model of segmental tunnel structure and the 2-dimension plane strain model (with 6 segments) in Plaxis software can be shown in Figure 4.

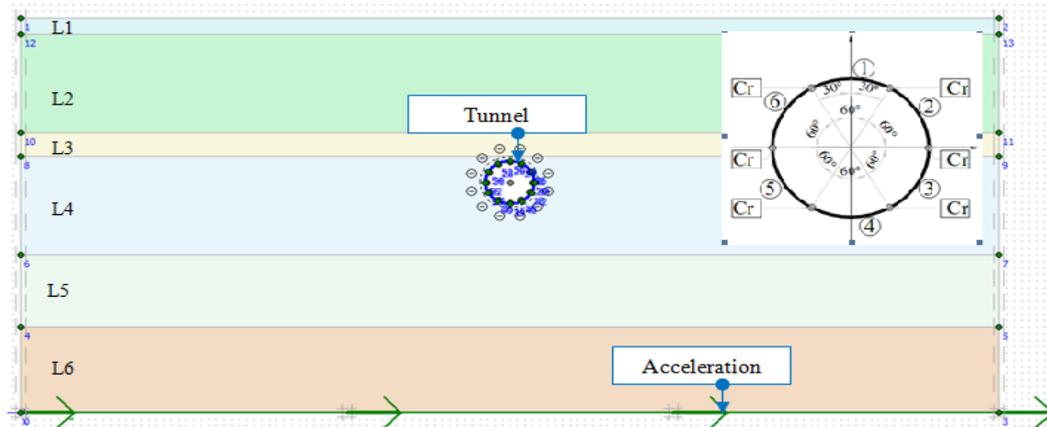


Figure 4. 2D plane strain model in Plaxis software

### 3. Earthquake time history

Earthquake time history input are artificial accelerations, which is generated by PG02, a program was written on Matlab. This program is a random simulation method

based on Yamamoto's regression equation, randomly generating artificial acceleration with a same target spectrum.

The target spectrum is determined by Vietnamese National Standard TCVN 9386-2012 with Ba Dinh district: the peak reference acceleration:  $a_{gR} = 0.0976g$ ; the important coefficient:  $\gamma_I = 1.0$ ; site classification: A class.

Using PG02 to generate 18 accelerations (denoted from bd01\_01a to bd01\_18a) as shown in Figure 5 to Figure 22.

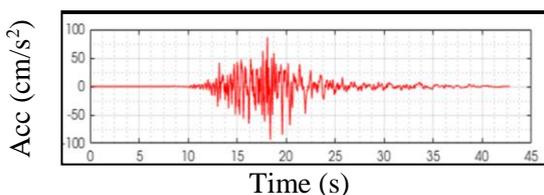


Figure 5. Acceleration *bd01\_01a*

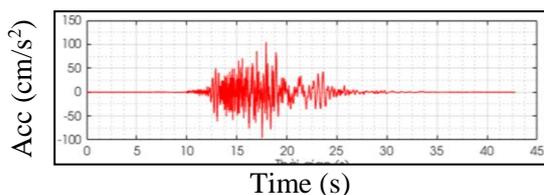


Figure 6. Acceleration *bd01\_02a*

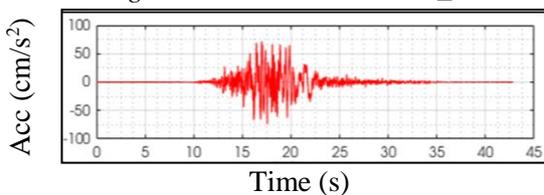


Figure 7. Acceleration *bd01\_03a*

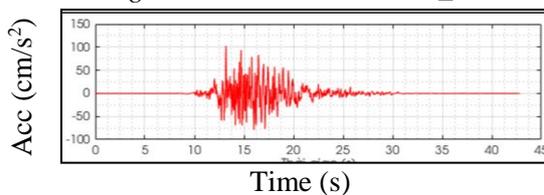


Figure 8. Acceleration *bd01\_04a*

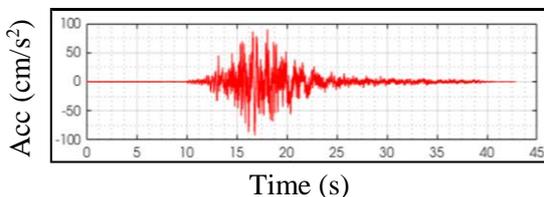


Figure 9. Acceleration *bd01\_05a*

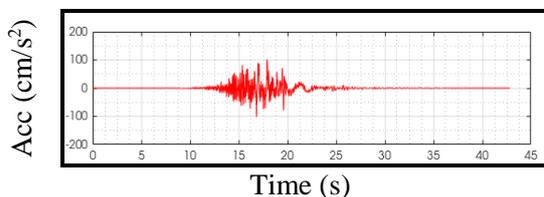


Figure 10. Acceleration *bd01\_06a*

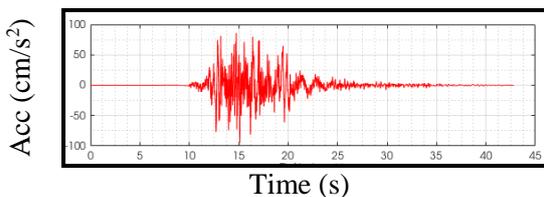


Figure 11. Acceleration *bd01\_07a*

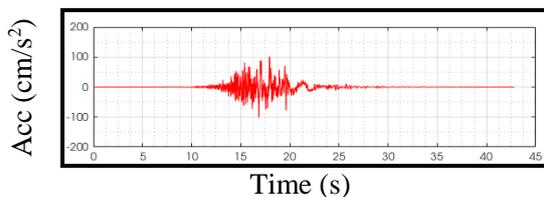


Figure 12. Acceleration *bd01\_08a*

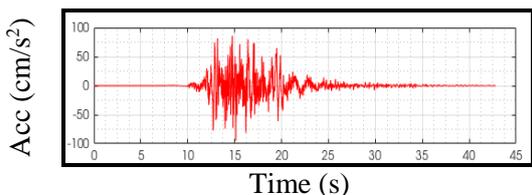


Figure 13. Acceleration *bd01\_09a*

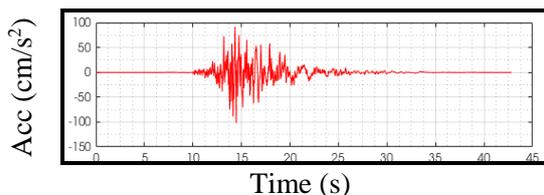


Figure 14. Acceleration *bd01\_10a*

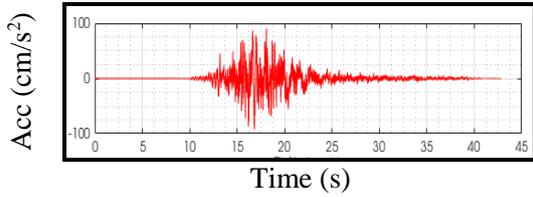


Figure 15. Acceleration bd01\_11a

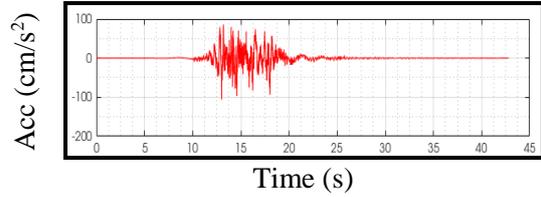


Figure 16. Acceleration bd01\_12a

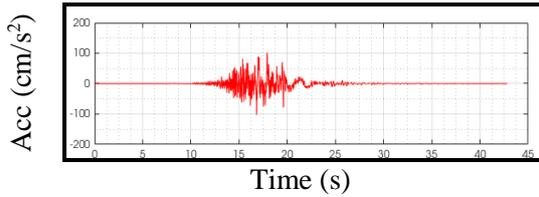


Figure 17. Acceleration bd01\_13a

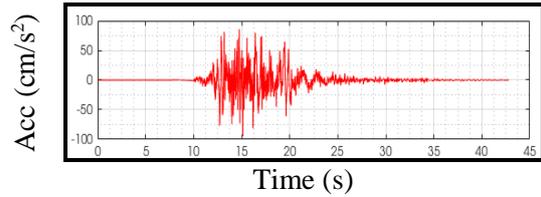


Figure 18. Acceleration bd01\_14a

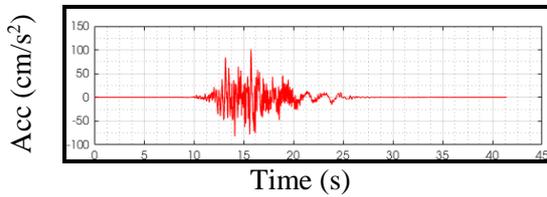


Figure 19. Acceleration bd01\_15a

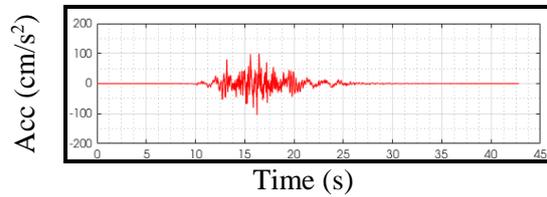


Figure 20. Acceleration bd01\_16a

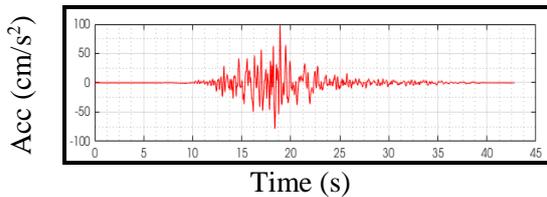


Figure 21. Acceleration bd01\_17a

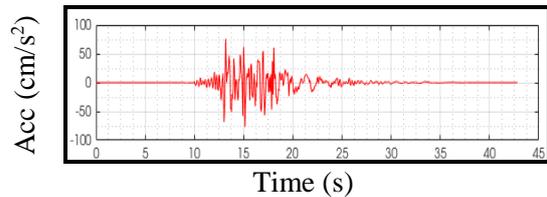


Figure 22. Acceleration bd01\_18a

The responses of 18 accelerations are shown in Figure 23.

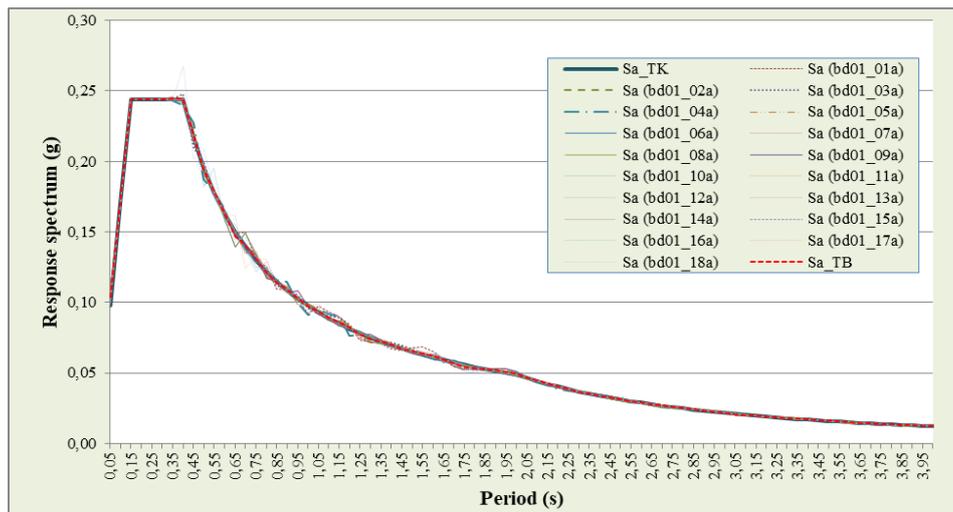


Figure 23. Response spectrum of artificial accelerations are generated by PG02

## 4. Results

The maximum envelope of inner force (bending moment, shear force and normal force) are shown in Table 3. In this table, PGA, PGV,  $a_{RMS}$ , IA,  $t_{5-95}$  respectively are peak ground acceleration, peak ground velocity, root mean square acceleration, intensity of Arias, time duration of strong motion.

Table 3. Table of max inner forces results

Artificial acceleration	Parameters of acceleration					Max. inner forces		
	PGA (cm/s <sup>2</sup> )	PGV (cm/s)	$a_{RMS}$ (cm/s <sup>2</sup> )	IA (cm/s)	$t_{5-95}$ (s)	Bending moment (kNm)	Shear force (kN)	Normal force (kN)
bd01-01a	93.73	6.21	25.63	10.800	9.28	138.96	105.08	765.54
bd01-02a	104.57	6.62	25.71	12.500	10.62	135.19	102.67	764.91
bd01-03a	73.69	6.89	27.99	9.450	6.78	138.98	105.61	765.54
bd01-04a	102.86	6.41	30.84	12.700	7.51	138.82	103.92	766.73
bd01-05a	92.15	8.05	27.74	10.600	7.73	140.02	106.45	766.91
bd01-06a	102.64	7.87	30.29	9.900	6.09	138.41	104.80	769.77
bd01-07a	94.65	7.53	29.15	11.700	7.72	138.50	105.12	768.06
bd01-08a	102.01	5.61	27.58	9.500	7.02	134.25	101.53	763.17
bd01-09a	105.74	7.93	32.82	10.900	5.70	142.04	105.70	769.45
bd01-10a	101.60	6.03	27.95	9.900	7.13	135.30	102.99	765.32
bd01-11a	104.24	6.49	26.95	9.900	7.67	136.07	103.28	767.08
bd01-12a	98.04	6.31	24.89	8.900	8.06	137.16	103.67	764.33
bd01-13a	76.83	6.86	28.99	12.200	8.16	140.42	106.26	764.62
bd01-14a	93.59	7.54	28.95	11.000	7.36	140.31	106.08	765.56
bd01-15a	88.56	8.31	28.85	9.500	6.43	136.96	103.17	768.53
bd01-16a	101.51	7.24	29.54	14.400	9.28	138.60	103.55	769.30
bd01-17a	99.88	8.18	30.89	10.200	5.98	142.33	107.34	769.57
bd01-18a	76.57	7.84	25.85	8.600	7.25	136.40	102.27	764.63
<b>Mean</b>	<b>95.16</b>	<b>7.11</b>	<b>28.37</b>	<b>10.70</b>	<b>7.54</b>	<b>138.26</b>	<b>104.42</b>	<b>766.61</b>

Statistical characteristics of max inner forces results are determined and presented in Table 4. Notice the ratio between standard deviation ( $\sigma$ ) and mean ( $\mu$ ), the acceleration has negligible influence on normal force. Histogram of max. bending moment and max. shear forces are shown in Figure 23 and Figure 24 respectively.

Table 4. Table of results

Row	Random variable	Unit	Mean ( $\mu$ )	Standard deviation ( $\sigma$ )	$\mu/\sigma$ (%)	The range of random variable	
						( $\mu-2\sigma$ )	( $\mu+2\sigma$ )
1	Max. bending moment	kNm	138.26	2.29	1.66%	133.68	142.84
2	Max. shear force	kN	104.42	1.64	1.57%	101.14	107.70
3	Max. normal force	kN	766.61	2.07	0.27%	762.47	770.75

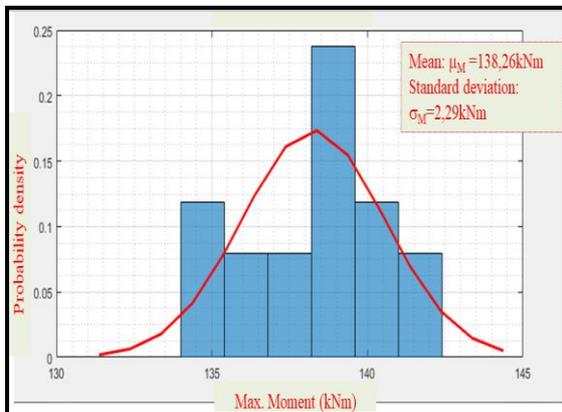


Figure 24. Histogram of max. bending moment

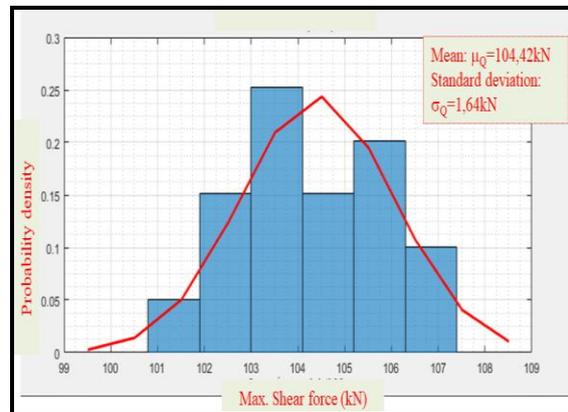


Figure 25. Histogram of max. shear forces

## 5. Conclusion

By above researches can be received some conclusions such as:

- Acceleration data set created by the PG02 program (18 accelerations) in accordance with Vietnamese National Standard TCVN 9386-2012 and suitable for seismic conditions of Ba Dinh district. These accelerations can be used to analyze the dynamics of earthquake-resistant underground structures.

- Although the peak of bd01\_03a, bd01\_13a, bd01\_18a accelerations are smaller than the rest, though, the internal forces results of the 3 cases are not significantly different from results of others. Therefore, the peak ground acceleration value can be considered as one of the important factors affecting the internal force of the tunnel besides some other acceleration factors (PGV,  $a_{RMS}$ ,  $t_{5-95}$ ...). The effects of these factors on the behaviour of tunnel lining need to be investigated in more detail.

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## PHÂN TÍCH KẾT CẤU VỎ HÀM DẠNG LẮP GHÉP CHỊU TÁC DỤNG CỦA ĐỘNG ĐẤT VỚI GIA TỐC NHÂN TẠO

**Tóm tắt:** Bài báo này nhằm mục đích xây dựng bộ gia tốc nhân tạo phù hợp với điều kiện thành phố Hà Nội bằng cách sử dụng chương trình PG02, chương trình được xây dựng dựa trên hệ phương trình hồi quy của Yamamoto và phổ phản ứng mục tiêu theo Tiêu chuẩn TCVN 9386-2012. Sử dụng bộ số liệu giả đồ gia tốc đã xây dựng để tính toán kết cấu hầm của dự án Tuyến metro số 3 (Nhón - Ga Hà Nội) chịu tác dụng của động đất bằng chương trình Plaxis2D. Các mối nối giữa các phân tố vỏ hầm được mô hình hóa theo giả thiết của Jassen. Kết quả cho thấy, giá trị gia tốc đỉnh chỉ là một trong những yếu tố ảnh hưởng đến nội lực của đường hầm bên cạnh một số yếu tố gia tốc khác (như: vận tốc đỉnh, gia tốc hiệu dụng, cường độ Arias, thời gian duy trì dao động mạnh).

**Từ khóa:** Tính toán công trình chịu động đất; vỏ hầm lắp ghép; giả đồ gia tốc nền nhân tạo; liên kết nửa cứng.

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